

Attosecond metrology: from electron capture to future signal processing

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The accurate measurement of time lies at the heart of experimental science, and is relevant to everyday life. Extending chronoscopy to ever shorter timescales has been the key to gaining real-time insights into microscopic phenomena, ranging from vital biological processes to the dynamics underlying high technologies. The generation of isolated attosecond pulses in 2001 allowed the fastest of all motions outside the nucleus — electron dynamics in atomic systems — to be captured. Attosecond metrology has provided access to several hitherto immeasurably fast electron phenomena in atoms, molecules and solids. The fundamental importance of electron processes for the physical and life sciences, technology and medicine has rendered the young field of attosecond science one of the most dynamically expanding research fields of the new millennium. Here, we review the basic concepts underlying attosecond measurement and control techniques. Among their many potential applications, we focus on the exploration of the fundamental speed limit of electronic signal processing. This endeavour relies on ultimate-speed electron metrology, as provided by attosecond technology.

Attosecond science represents the culmination of the long-standing investigation of fast-evolving phenomena in nature. After the concepts of pump–probe spectroscopy¹ and optical synchronization² were introduced in the nineteenth century, subsequent progress in improving the temporal resolution of time-resolved measurements was dictated by the development of light sources capable of producing ever-shorter pulses and of techniques for their measurement. Several technological revolutions were required to advance ultrafast science from the nanosecond scale, which can be accessed by incoherent light sources, to the femtosecond regime, and eventually to the attosecond regime. The laser^{3,4} (for which Basov, Prokhorov and Townes were awarded the Nobel Prize in Physics in 1964) provided the basis for all these advances, thanks to its ability to emit perfectly sinusoidal light waves over many seconds, which consist of quadrillions (10^{15}) of identical wave cycles. This coherence opened the door for measuring time over long periods and brief intervals with unprecedented precision and resolution, respectively.

Perturbative nonlinear optical effects^{5,6} (for which Bloembergen was awarded the Nobel Prize in Physics in 1981) allow the optical properties of materials, such as their refractive index and absorptivity, to be varied as a function of the cycle-averaged intensity of intense laser radiation. Some of these changes can be harnessed to create light modulators, which alter the phase and/or amplitude of transmitted or reflected laser light in proportion to its intensity. Integrating such a device in a broadband laser oscillator permits the eigenmodes of the laser cavity modes to be phase locked. A second revolution, namely in nonlinear optics⁷, thus led to the generation of femtosecond laser pulses⁸. By the turn of the millennium and some 15 years after the seminal report on three-cycle optical pulses by Shank and co-workers⁹, the evolution of femtosecond technology approached its ultimate limit — the wave cycle¹⁰; this was achieved through realizing broadband dispersion control using chirped multilayer mirrors¹¹ (Fig. 1). The envelope of the fastest, few-femtosecond laser pulses is short enough to temporally resolve any molecular dynamics¹² (for which Zewail was awarded the Nobel Prize in Chemistry in 1999), but it is insufficient to capture atomic-scale electronic motion.

Strong-field interactions driven by few-cycle light pulses¹⁰ enabled the electronic responses of matter to be controlled and

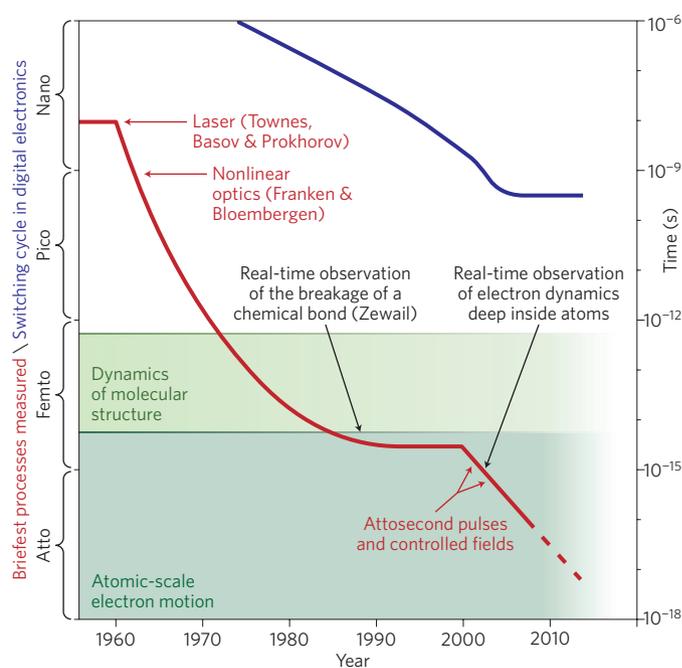


Figure 1 | Evolution of ultrafast science and digital electronics. Briefest measured time intervals (lower red line) and shortest switching cycle (inverse of the clock rate) of digital processors (upper blue line). Discontinuities in the derivative of the briefest measured interval against year curve indicate revolutions in ultrafast metrology. In the early 1960s, coherent light waves generated by lasers and nonlinear optical effects were used to produce ultrashort pulses from these waves. At the beginning of the new millennium, attosecond pulse generation and measurement¹⁸ were realized, and controlled light fields for precision attosecond control²⁸ and metrology³⁴ were generated.

measured within an optical cycle, that is, on an attosecond timescale. Just as cycle-averaged-intensity-driven perturbative nonlinear optics had led to femtosecond pulses, nonperturbative

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nonlinear optical effects governed by a strong, oscillating field, such as above-threshold ionization¹³ and high-order harmonic generation (HHG)^{14–17} spawned extreme ultraviolet (XUV) light pulses lasting less than 1 fs (ref. 18); this represents the latest revolution in ultrafast science^{19,20} (Fig. 1).

The field–matter interactions underlying attosecond technology are sensitive to the subcycle evolution of the optical field, $F_L(t) = F_0 a(t) \exp[-i(\omega_L t + \varphi_{CE})] + \text{c.c.}$, where F_0 is the peak electric field, $a(t)$ is the normalized amplitude envelope, ω_L is the carrier frequency, φ_{CE} is the carrier-envelope phase (CEP) and c.c. is the complex conjugate. Some four decades after the invention of the laser, the field oscillations ‘underneath’ the amplitude envelope became relevant²¹. The timing of field oscillations with respect to the pulse peak set by the CEP fluctuates in a femtosecond laser²² simply because the (perturbative) nonlinear optical effects responsible for laser mode locking are insensitive to the CEP. Broadening of the mode-locked laser spectrum to a full octave and self-interference of the radiation with its second harmonic²³ provided access to the quasi-periodic evolution of the CEP²⁴ in the emitted femtosecond pulse train and allowed it to be locked to a radiofrequency reference^{25,26}. The resultant phase-coherent link between the radiofrequency signals and the optical radiation allowed this locked optical frequency comb to connect atomic transitions, which have the potential to be used as optical frequency standards, with radiofrequency electronic signals driving clocks²⁷ (Hänsch and Hall were awarded the Nobel Prize in Physics for this work in 2005). The radiofrequency control of the mode-locked frequency comb and subsequent amplification and pulse compression provided intense, CEP-stabilized (that is, waveform-controlled), few-cycle light pulses²⁸.

Attosecond pulse generation and measurement

The electric field of an intense waveform-controlled, few-cycle light pulse²⁸ exerts a force on electrons that rivals intra-atomic (Coulomb) forces and can be varied in a controlled fashion on the electronic timescale. This attosecond force can be shaped within the wave cycle to an extent that depends on the relative bandwidth, $\Delta\omega/\omega_L$, of the light pulse. For a sub-octave bandwidth ($\Delta\omega/\omega_L < 1$), adjustment of the CEP provides a means of shaping the field evolution within the field cycle. Although it is quite weak even for a two-cycle pulse (Fig. 2a), this shaping is crucial for reproducible generation of isolated attosecond pulses by HHG²⁹ (Fig. 2b,c). Control of the field evolution within the wave cycle permits attosecond control of the three steps involved in the emission of attosecond XUV pulses — tunnel ionization, excursion of the quasi-free electron and its recollision with the parent ion^{30–33}. It thus enables the parameters of attosecond laser pulses to be precisely reproduced from one pulse to the next.

Waveform control is equally important for temporal characterization. In fact, it is the controlled, attosecond variation of the laser electric field that maps the temporal profile of the attosecond pulse to a final momentum distribution of photoelectrons³⁴ in the light-field-driven (or attosecond) streak camera^{35,36} (Fig. 3). Recording photoelectron spectra for varying timings of the attosecond pulse with respect to the streaking field provides complete information about the temporal intensity profile and chirp of the attosecond pulse as well as the electric field in a few-cycle wave^{37–40}.

Trains of attosecond pulses and their first applications

Electron dynamics confined to less than one laser period can also be time resolved by attosecond pulse trains, which were first generated in 2001^{41–43}. Alternatively, the harmonic emission produced by the recolliding electron may also serve as a probe⁴⁴. In these measurements, the dynamics is re-triggered each cycle by the next attosecond burst or by the next period of the strong laser

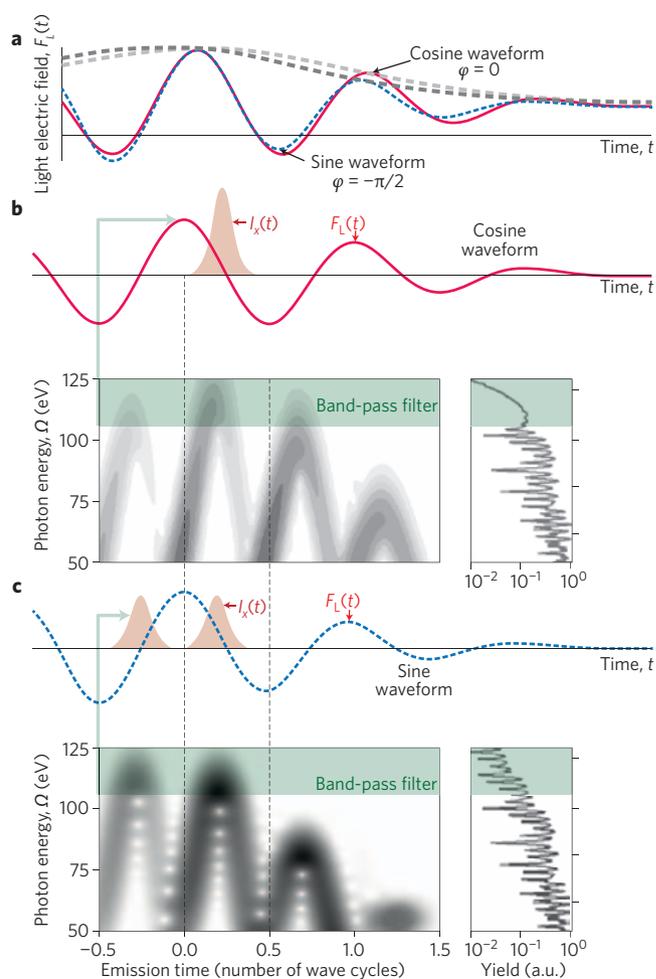


Figure 2 | Prediction of attosecond XUV pulses. a–c, Computations by V. Yakovlev predicted the emission of attosecond XUV pulses from neon atoms irradiated by NIR laser fields (wavelength, 750 nm). These pulses contain two oscillation cycles within the 5-fs full-width at half-maximum of their intensity envelope (a) for a cosine (red solid lines in a and b) and sine (blue dashed lines in a and c) waveforms; despite the fact that these two waveforms differ only slightly, they are predicted to lead to an isolated XUV pulse and a twin attosecond XUV pulse, respectively. Figure courtesy of V. Yakovlev. Figure adapted with permission from ref. 125 © 2007 NPG.

field. Consequently, the physical observables are accumulated over many sub-laser-cycle pump–probe exposures, and hence variations in physical parameters (such as the laser field amplitude and the probe pulse duration) over this multicycle signal accumulation should be minimized. In a series of carefully performed experiments^{45–50}, the attosecond dynamics of electron wave packets launched by an attosecond pulse train in atoms and molecules were traced by the multicycle field previously used to generate the attosecond pulse train. Subcycle processes periodically triggered by multicycle fields in atoms and molecules can be efficiently interrogated by the sub-femtosecond recolliding electron wave packets extracted from the sample under scrutiny by strong-field ionization. In this powerful approach, the multicycle wave both generates the recolliding electron probe and triggers the subcycle process under study in a correlated fashion, leaving no room for any timing jitter between the pump and the probe. The generated high-order harmonics and photoelectrons provide unprecedented insight into the attosecond electron dynamics and accompanying molecular dynamics^{51–65}.

Tracing electrons with isolated attosecond pulses

Waveform-controlled, few-cycle laser pulses²⁸ and the reproducible isolated attosecond pulses they spawn^{34,66,67} constitute an enabling technology for both precision attosecond metrology of light signals and real-time access to a vast variety of electron processes that unfold on the attosecond timescale and extend over the femtosecond timescale. Figure 4 displays these tools at the heart of a state-of-the-art attosecond system. Sub-4-fs, near-infrared (NIR), 750-nm-carrier-wavelength laser pulses produce sub-100-attosecond XUV pulses in the 100-eV photon energy range via HHG in neon gas. An attosecond electron streak camera records the streaking spectrogram (shown in the inset in Fig. 4), which allows both the sub-4-fs laser waveform and the 72 as XUV pulse (depicted on the optical axis) to be retrieved. Arriving in perfect synchrony with each other, they (or their slightly longer predecessors) allow a variety of pump–probe techniques to be performed, including attosecond streaking^{68,69} and tunnelling spectroscopy⁷⁰ in which the XUV pulse is used as the trigger and the controlled laser field as the probe. They also provide real-time insight into multi-electron relaxation processes in highly excited atoms, such as a cascaded Auger decay⁷⁰ and intra-atomic electron correlations implying a delay in photoemission⁶⁹.

In a similar scheme, attosecond photoelectron spectroscopy provides access to details of atomic ionization^{71,72} as well as structural and electronic wave-packet dynamics in simple molecules^{73,74}. Alternatively, strong-field processes induced by a controlled laser waveform can be tracked by attosecond transient absorption spectroscopy by using the XUV pulse as the probe⁷⁵. Attosecond transient absorption measurements on krypton atoms ionized by a near-single-cycle NIR field have revealed for the first time electron tunnelling within a fraction of a half wave cycle, an instantaneous optical-field-induced Stark shift of valence levels, and the emergence of coherent valence electron wave packet dynamics in an ion ensemble⁷⁶. These experiments provide compelling evidence that the basic attosecond tools and techniques work well and that they have become mature enough for their application to extend to condensed matter.

Attosecond physics of condensed matter

Attosecond processes in solids were first accessed experimentally by using a short-lived core hole in an adsorbed sulphur atom as a clock⁷⁷. The first attosecond time-resolved study⁶⁸ was performed on monocrystalline tungsten using attosecond streaking³⁵. It revealed that electrons originating from localized core states of tungsten arrived at the tungsten surface with a ~100 as delay relative to those freed from delocalized conduction-band states. In contrast, for monocrystalline magnesium, photoelectrons originating from the core and valence-band states arrived simultaneously at the surface, within the experimental uncertainty of 20 as (ref. 78). Comparison of these experimental results with theoretical investigations^{79–86} suggests that the observed delays originate from electron propagation. If so, the new method may be dubbed attosecond electron-propagation chronoscopy; it appears to be a sensitive probe of the high-energy band structure and a promising approach for exploring atomic-scale electron transport phenomena near surfaces.

Internal strong-field photoionization (breakdown) of insulators⁸⁷ is expected to follow the instantaneous excitation field and hence be CEP dependent, as predicted earlier for photoemission from metal nanostructures⁸⁸. The first experimental observation of strong-field photoemission from tungsten nanotips⁸⁹ confirmed this prediction, as did a more recent study of gold nanotips⁹⁰. A subsequent investigation⁹¹ of strong-field emission from a plasmonic (gold) nanotip at local field strengths of approximately $< 2 \text{ V \AA}^{-1}$ established a new effect — a very short localization

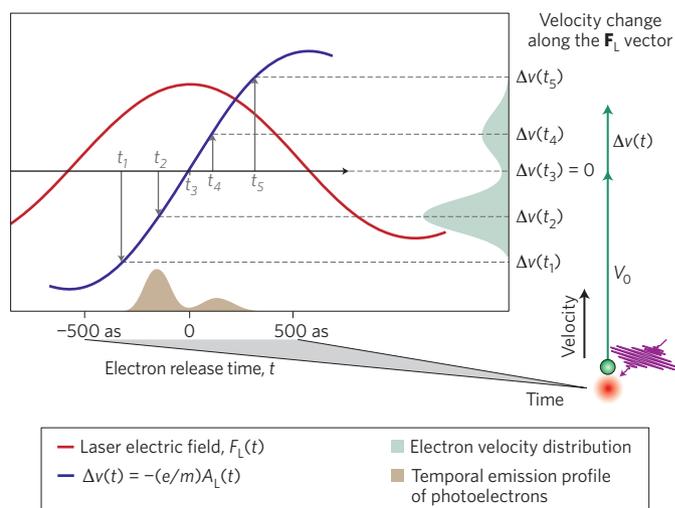


Figure 3 | Concept of light-field-driven attosecond streaking.

Photoelectrons released by an attosecond XUV pulse in the presence of a strong linearly polarized laser field (red line) parallel to the electric field vector suffer a change in their velocity that is proportional to the vector potential of the field (blue line) at the moment of release. Here, $\Delta v(t)$ is proportional to the vector potential of the electric field, $A_L(t)$. This change in the final velocity is monotonic within a half wave cycle of the field, and maps the intensity profile of the sub-femtosecond XUV pulse to a corresponding final velocity distribution of photoelectrons. Recording these ‘streaked’ photoelectron spectra as a function of time delay with respect to the streaking field yields a streaking spectrogram (see Fig. 4), from which the attosecond XUV pulse profile and chirp as well as the laser waveform can be retrieved. Figure adapted with permission from ref. 20; © 2009 APS.

radius of the nanoplasmonic field at the tip permits an electron to escape from the nanolocalized region within a fraction of an optical cycle (that is, on a timescale of hundreds of attoseconds), effectively suppressing ponderomotive oscillations. As Stockman *et al.*⁹² proposed, this allows a photoelectron ejected by an attosecond XUV pulse to probe directly the local electric field; this is in contrast with gas-phase attosecond streaking experiments³⁴, which probe the vector potential of the local electric field (that is, its time integral). Attosecond probing of nanoscopic electric fields will provide direct access to ultrafast nanoplasmonics in space and time.

These novel attosecond techniques may be instrumental in investigating ways to overcome the speed limits of contemporary digital electronics and explore the ultimate limits of electron-based signal processing.

Frontiers of electronic signal processing

The basic building blocks of contemporary digital electronics are metal–oxide–semiconductor field-effect transistors (MOSFETs)⁹³. Although high-speed MOSFETs function up to cutoff frequencies f_{cutoff} in the approximate range 100 GHz–1 THz (refs 94–103), the maximum speed (the clock rate in engineering terminology) of processors has been limited to $f_{\text{processor}} \approx 3 \text{ GHz}$ for more than a decade (see Fig. 1). This limitation is a result of the charging time, $\tau_{\text{charging}} \lesssim 100 \text{ ps}$ of the interconnect wires that couple the transistors to form a processor; specifically, $f_{\text{processor}} \approx \tau_{\text{charging}}^{-1}$ (Fig. 5; for more details, see Box 1). Yet another limitation originates from heat dissipation, which mainly occurs in contemporary digital electronics when a transistor recharges the interconnect wire. The energy dissipated during this process per switching cycle for a long (~5 mm) interconnect is of the order of $Q_{\text{switch}} \approx (1/2)$

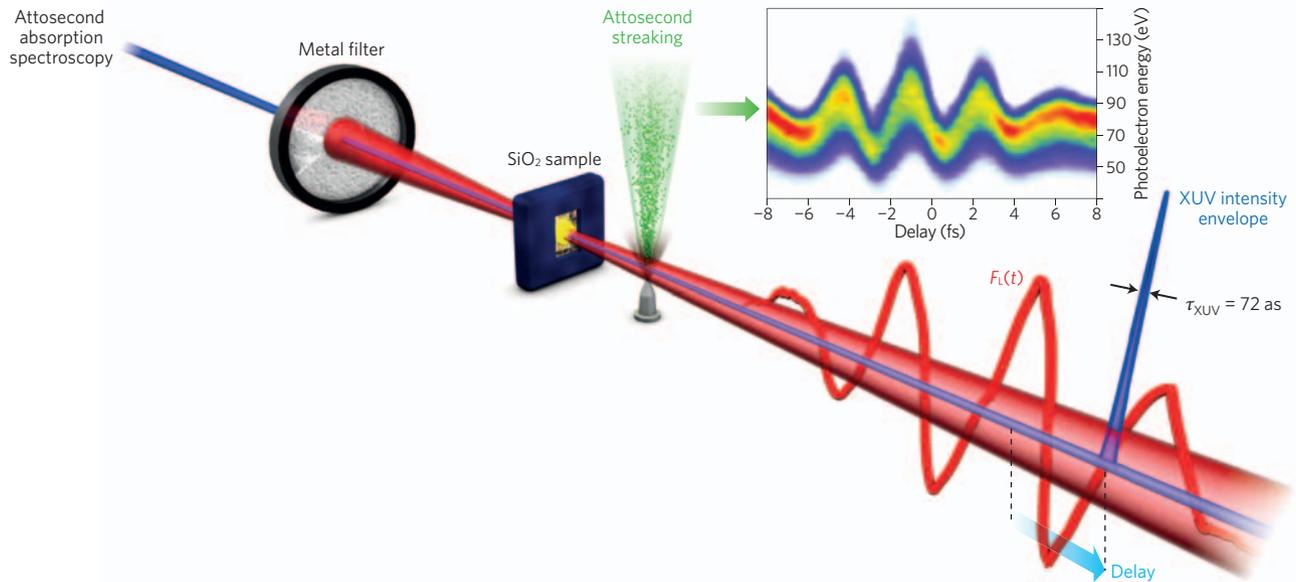


Figure 4 | Tools of attosecond metrology and spectroscopy. Sub-4-fs, sub-1.5-cycle NIR laser pulses and synchronized near-70-as XUV pulses retrieved from the attosecond streaking spectrogram (shown in the inset). Simultaneous streaking and attosecond probe (here, absorption) spectroscopy permit attosecond timing of the attosecond snapshots (here, transient absorption spectra) to the strong excitation field triggering electron motion (as shown in Fig. 6). Figure adapted with permission from ref. 110 © 2013 NPG.

$C_{\text{interconnect}}(\Delta U_{\text{gate}})^2 \approx 1$ fJ. The processor clock rate is determined by long interconnects, whereas the average energy per switch per transistor is determined by a typical (~ 500 μm) interconnect, and is an order of magnitude smaller ($Q_{\text{switch}} \approx 0.1$ fJ). This gives an upper limit for the power consumption per processor $P_{\text{processor}} \approx N_t f_{\text{processor}} Q_{\text{switch}} \approx 300$ W, where $N_t \approx 10^9$ is the number of transistors in the processor. This upper limit is several times higher than typical power consumptions ($P_{\text{processor}} \approx 100$ W), because not all transistors switch all the time. Such a high power consumption presents problems both for heat management and the combined energy cost of existing computers that already significantly load the power grid, constituting another severe challenge for scaling current digital electronics to much higher clock rates and transistor numbers.

Optical on-chip interconnects are promising for circumventing these limitations¹⁰⁴. As these interconnects need to be the same size as the transistors themselves, deeply subwavelength structures that rely on plasmonic nanoconfinement are required^{105–107}. The bandwidth of nanoplasmonic structures extends over the entire visible spectrum into the mid-infrared range¹⁰⁵, resulting in a response time of $\tau_{\text{response}} \lesssim 1$ fs. Hence, future plasmonic interconnects may, in principle, open the door for scaling the signal processing (clock) frequency towards the petahertz frontier, and research and development of these systems may benefit from the attosecond techniques described in the previous section. However, the speed of MOSFETs, which is limited by the mobility, recombination time and plasma frequency of the carriers^{95–99,102,103}, is unlikely to substantially exceed ~ 1 THz. Hence, novel concepts are required to approach the petahertz frontier.

The response time of a physical system is determined by its bandwidth according to $\tau_{\text{min}} \lesssim \Delta\omega^{-1}$. To use this bandwidth without major losses, the signal should spectrally be confined within the bandgap, which imposes another condition, $\Delta\omega \lesssim \Delta\epsilon_g$; this implies that $\tau_{\text{min}} \lesssim \Delta\omega^{-1}, \Delta\epsilon_g^{-1}$. Dielectrics such as silica and alumina and wide-bandgap semiconductors such as GaN and diamond with bandgaps in the approximate range of 5–10 eV possess the fastest responses, potentially of the order of several hundred attoseconds.

However, they require strong fields to induce changes in their electronic and optical properties. The recent demonstration of HHG induced by a strong ($F_0 = 0.2\text{--}0.6$ V \AA^{-1}) mid-infrared field in a crystal of the wide-bandgap semiconductor ZnO (ref. 108) up to frequencies in the VUV range has revealed nonlinear photocurrents in the solid with an oscillation time on a ~ 100 as timescale.

Indirect experimental evidence of attosecond photogeneration of carriers in silica was provided by an observed change in the ellipticity of a laser pulse¹⁰⁹. These experiments also suggest that for sufficiently short pulses ($\lesssim 40$ fs), the electron dynamics is not distorted by collisions.

The attosecond response of wide-bandgap materials has recently been confirmed in an attosecond time-resolved experiment seeking to track changes in the band structure and/or population dynamics induced in silica by a strong, few-cycle NIR field¹¹⁰. An attosecond XUV probe pulse traversing the sample promoted electrons from the L-shell of silicon to the conduction band of silica. Figure 6 shows a line out of the recorded transient

Box 1 | Clock rate in contemporary semiconductor electronics

The interconnect-limited processor speed (clock rate) is given by $f_{\text{processor}} = \tau_{\text{charging}}^{-1} = I_{\text{drive}} / (C_{\text{interconnect}} \Delta U_{\text{gate}})$, where $C_{\text{interconnect}}$ is the interconnect capacitance, ΔU_{gate} is the gate potential difference and I_{drive} is the drive current produced by the transistor. Modelling the interconnect as a cylinder of radius a and length L in a medium of permittivity ϵ , results in $C_{\text{interconnect}} \approx \epsilon L / [2 \ln(L/a)]$, where $L \gg a$ (ref. 122). Using realistic parameters¹²³, $I_{\text{drive}} = 30$ μA and $\Delta U_{\text{gate}} = 0.3$ V, and assuming $L \approx 1$ mm, $\epsilon \approx 6$ and $a \approx 30$ nm, we obtain $f_{\text{processor}} \approx 3$ GHz. This is very close to the actual processor speed limit and is two orders of magnitude slower than the transistor speed. Dissipation of electrostatic energy during recharging of the interconnects was found to reduce the energy efficiency of the processor by three orders of magnitude with respect to that of the transistors¹²⁴.

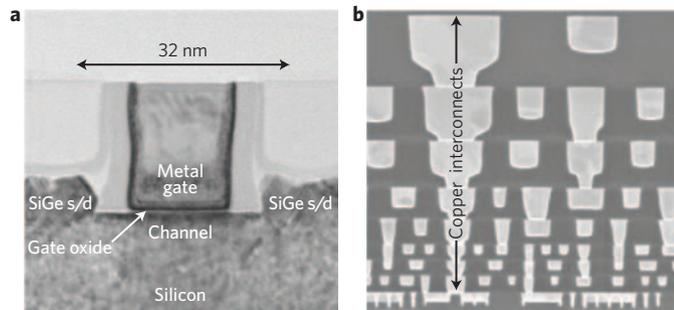


Figure 5 | Electron micrographs of Intel processor chip and MOSFETs in it. **a**, Transistor cross-section, where “s/d” indicates the source and drain. **b**, Copper interconnect wires (one of which is labelled) are visible in the processor cross-section (vertical size is a few millimetres). The MOSFETs are at the very bottom of this micrograph. Figure adapted from ref. 126 © 2011 Intel.

absorption spectrum at the band edge; it exhibits an instantaneous, highly reversible, transient decrease in the XUV absorptivity that oscillates in synchrony with the strong field. This suggests that this dynamics follows the instantaneous electric field, and is dominated by instantaneous changes in the local density of the conduction-band states and its virtual population rather than real transfer of population, which would survive for picoseconds (see also the caption of Fig. 6c). Note that the total conduction-band population (the sum of the virtual and real populations) is given by equation (10) in the supplementary information of ref. 110 (see also the next section). The dominance of the virtual conduction band population over the real conduction band population is also corroborated by the theoretical prediction shown in Fig. 6c. The real population can be identified as the conduction-band population that survives for delays exceeding the pulse duration. This residual value happens to be much smaller than the peak value of the total transient population, which is thus predicted to be dominated by virtual population. This conclusion appears to contradict that drawn from the recent analysis of second-harmonic emission from dielectrics¹¹¹. It has far-reaching implications for potential signal processing and metrology applications.

Controlling the electric and optical properties of dielectrics at optical frequencies

Unlike in metals, electric fields can penetrate and charge gradients can build up in semiconductors as a result of their moderate bandgaps ($\Delta_g \lesssim 1$ eV). This forms the basis of contemporary digital electronics^{93–96,112}. The above-mentioned recent attosecond study on silica¹¹⁰ revealed that strong optical fields can substantially modify the electronic structure of wide-bandgap materials on a near-1-fs timescale, making them promising for developing a fundamentally new approach to electric and photonic signal manipulation, which may be largely free from the limitations of contemporary MOSFETs discussed above.

For fields with strengths approaching the critical field strength, $F_{\text{crit}} = \Delta_g/ea$ (where a is the lattice constant and e is the electronic charge) varying adiabatically to fulfil the condition $\omega_L \ll \Delta_g/\hbar$ (where \hbar is the reduced Planck constant) electronic states of the solid are predicted to undergo Wannier–Stark (WS) localization¹¹³ within approximately one unit cell of the crystal. For dielectrics such as silica and alumina with $\Delta_g \approx 9$ eV, F_{crit} will be approximately 2 V \AA^{-1} , and the condition $\omega_L \ll \Delta_g/\hbar$ will be satisfied up to near-infrared and visible frequencies. WS localization and formation of the WS energy ladder then occurs. The energy of a WS state residing at a certain site $l = 1, 2, \dots$ (where l is the site number

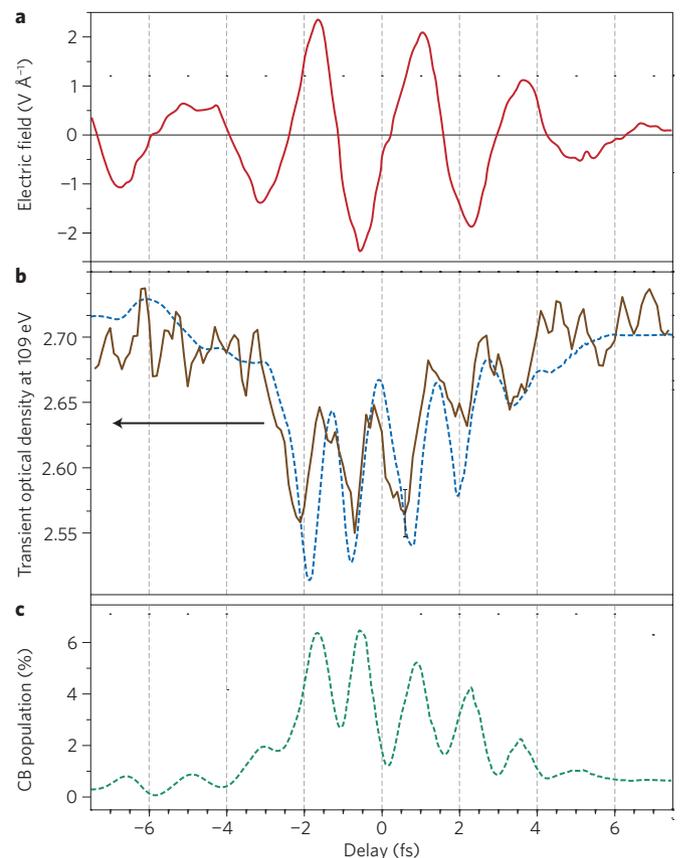


Figure 6 | Attosecond time-resolved, strong-field-induced effects in SiO₂. **a**, Electric field of a few-cycle NIR laser pulse impinging on a SiO₂ sample, $F_L(t)$, as extracted from attosecond streaking (see Fig. 4). **b**, Transient change in the optical density integrated over a 1-eV bandwidth at $\hbar\omega = 109$ eV probed by the 72 as XUV pulse shown in Fig. 4 and timed to the NIR excitation field shown in **a** by simultaneous attosecond streaking. This allows the measured transient observable (in this case, the absorptivity) to be assigned to well-defined moments in the excitation field. Simultaneous attosecond probe spectroscopy and streaking thus provide unprecedented insight into strong-field electron processes. **c**, Computed transient evolution of the instantaneous population of (unperturbed) conduction-band (CB) states timed to the laser field. The dominant part of the conduction-band population, which oscillates as a function of the delay, is termed the virtual population in ref. 114 (it was originally introduced in refs 115–118). Figure adapted with permission from ref. 110 © 2013 NPG.

expressed in terms of the lattice period) of the lattice along the direction of the internal field F becomes $E_{l,n} = E_n - eaFl$, following the field variation adiabatically. (Here, E_n with $n = \{c, j\}, \{v, k\}$ is the offset of the j th and k th subbands of the conduction and valence bands, respectively; for simplicity, we suppress the subband indices j and k in the present discussion.) The adjacent levels in each WS ladder are separated by the Bloch frequency, $\omega_B = |eF|a/\hbar$. For $F \rightarrow F_{\text{crit}}$, by definition, $\hbar\omega_B \approx \Delta_g$, and hence the Bloch frequency will be in the ultraviolet range. At this point, according to $E_{l,n} = E_n - eaFl$, $E_{l,c}(F)$ and $E_{l,v}(F)$ will become nominally equal for $\Delta l = |l_c - l_v| = 1$; that is, the WS states residing at neighbouring sites in the conduction and valence bands will become degenerate in energy to undergo an anticrossing. The calculated level diagram for silica¹¹⁴ (see Fig. 7) reveals a large energy gap ΔE_1 at $\Delta l = 1$. The corresponding anticrossing gap is much larger than the NIR laser photon energy. This implies that the WS state belonging to the

lower anticrossing level remains fully occupied while adiabatically changing its wavefunction from the valence band to the conduction band (this is the well-known adiabatic exchange of quantum numbers). Consequently, the dynamics is largely reversible.

This gradual change can be quantified by projecting the actual filled, time-dependent valence-band states to zero-field conduction-band states (see equation (10) in the supplementary information of ref. 110). This projection results in the transient population of conduction-band electrons shown in Fig. 6c, and the corresponding valence-band holes. These electrons and holes can be interpreted as virtual carriers, similar to those responsible for virtual photoconductivity in semiconductors, which was theoretically predicted^{115–117} and experimentally observed¹¹⁸ over two decades ago. However, the analogy stops there. In the present case, the virtual carriers are produced by a nonresonant (adiabatic), strong-field (and thus, necessarily, nonperturbative) excitation; this contrasts with the early experiments in which the virtual carriers were excited by a near-resonant perturbative excitation. The virtual carriers make the system more polarizable in a static electric field^{115–117} and also at optical frequencies. If so, they can help qualitatively understand both the transient reflectivity shown in Fig. 3b of ref. 110 and the transient current presented in Fig. 3 of ref. 119. Note that our conclusion on the reversibility of the photoinduced changes in dielectrics is generally incompatible with perturbation theory. In particular, the reversibility is at odds with the analysis in ref. 120, because processes proceed in one direction only in any perturbation theory. Specifically, the population is transferred from the almost completely filled valence band to the weakly populated conduction band, and the photoinduced changes are not reversible — the probability of reverse transfer from the conduction band to the valence band decreases in proportion with the conduction-band population. Thus, in perturbation theory, the excited-state population should continuously increase with every half cycle of the field, in disagreement with both the experimental results and the theory presented in ref. 110.

In the originally introduced picture^{110,119}, the strong but deeply adiabatic optical fields create a new state of matter in which the states of the original valence and conduction bands are mixed and the spectrum shows the formation of WS ladders and their anticrossings. In addition, population transfer between the valence and conduction bands occurs reversibly (see Fig. 7). The most significant adiabatic population transfer occurs at $\Delta l = 1$. Consequently, the original bandgap of the dielectric disappears as the energies of the occupied and empty states overlap. Thus, the pronounced Fermi surface separating the filled and empty states disappears. Because of this bandgap collapse, such a non-equilibrium state has a high polarizability; in particular, the optical conductivity is over 18 orders of magnitude higher than that of the original dielectric, reaching levels typical of semimetals¹¹⁹ (it is still several orders of magnitude lower than the conductivity of a good metal). Such a non-perturbative phenomenon can

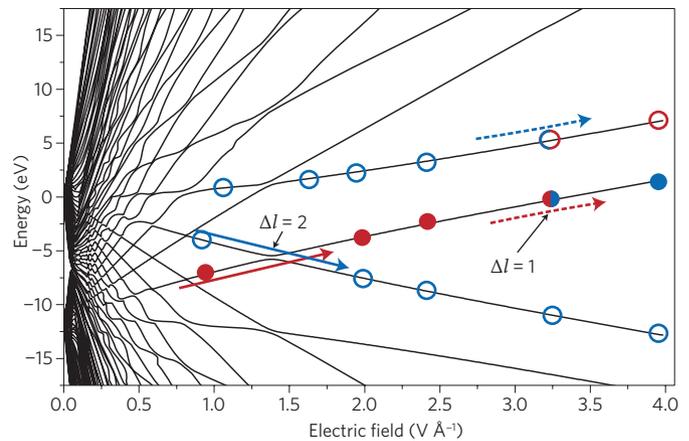


Figure 7 | Adiabatic energy spectra of valence and conduction bands for silica in strong fields. These are shown for a crystal with 50 unit cell thickness as a function of the electric field for an interband dipole moment $Z_{v,c}$ of 3 eÅ . The anticrossings with $\Delta l = 1$ and $\Delta l = 2$ are indicated. Red and blue circles denote levels with valence and conduction band wavefunctions, respectively. Closed and open circles represent filled and empty states, respectively. The solid crossed and dashed parallel arrows indicate level anticrossings passed diabatically and adiabatically, respectively. Figure adapted with permission from ref. 114 © 2014 NPG.

thus be termed semi-metallization. Note that the last anticrossing at $\Delta l = 1$ is only approached but not passed at the fields applied, as the field required for the full passage ($F_0 \lesssim 3.5 \text{ V Å}^{-1}$) exceeds the current breakdown threshold. If the $\Delta l = 1$ anticrossing were passed without breakdown, the dielectric would have undergone a full metallization transition.

Towards petahertz-scale solid-state technology

The nonlinear polarization induced by the instantaneous optical field can be used to modulate optical signals and electric currents via strong-field-induced changes in the reflectivity (or phase delay)¹¹⁰ and strong-field-induced charge separation¹¹⁹, respectively. The underlying physical mechanisms differ fundamentally from those responsible for signal processing in MOSFETs where real carriers transport electric current and dissipate heat. In contrast, the strong-field effects described above create predominantly virtual carriers and offer the potential to manipulate signals in a largely reversible fashion. Dissipation originates from only the residual (real) carriers left behind by the strong few-cycle field. Maximizing the ratio of the peak to residual density of carriers, $n_{\text{peak}}/n_{\text{res}}$ (~ 7 in Fig. 6c), would obviously minimize the dissipation per switching cycle and might provide a route to greatly increase the processing speed. An additional avenue to increase the energy efficiency of processing, albeit at the expense of a lower ultimate speed, is reducing the laser

Box 2 | Heat dissipation and power requirements of prospective 'dielectric electronics'

For processor applications, the power dissipated in a nanostructure is a critical issue. Note that most effects of high-field interaction with dielectrics are reversible, so that the absorbed power is returned to the field at the end of the pulse. In conventional processors, most heat is produced when a transistor recharges the interconnect wire, resulting in a dissipation energy per switching of $Q_{\text{switch}} \approx 1/2 C_{\text{interconnect}} (\Delta U_{\text{gate}})^2 \approx 1 \text{ fJ}$. In contrast, all-optical processors have no electrostatic charging of interconnect wires. In our case of a dielectric in a strong-pulse field, the heat released is equal to the excitation energy $\Delta_g \approx 10 \text{ eV}$ per real population of the electrons phototransferred from the valence band to the conduction band. This yields in a dissipation per switch of $Q_{\text{switch}} \approx \Delta_g \sigma A / e$, where σ is the transferred charge density and A is the cross-section of the excitation area. In experiments described in ref. 119, the phototransferred charge is $Q_p \approx 1 \text{ fC}$ per unit excitation cross-section ($\sim 3 \times 10^{-5} \text{ cm}^2$), which yields $\sigma \approx 3 \times 10^4 \text{ fC cm}^{-2}$. Plasmonic concentration makes it possible to produce an optical switch with a size of $\sim 10 \text{ nm}$, which is sufficiently small for large-scale integration. Assuming $A \approx 5 \text{ nm}^2$, we obtain $Q_{\text{switch}} \approx 10 \text{ aJ}$.

frequency with respect to bandgap, ω_i/Δ_g . This is expected to render processes more adiabatic (reversible). However, the interaction time should still remain shorter than the electron collision time ($\lesssim 50$ fs) to prevent dephasing^{105,109}. Because the underlying processes are largely adiabatic, which causes the absorbed power to be returned to the field at the end of the switching laser pulse, heat dissipation per switching may be much lower than that of conventional semiconductor electronics (see Box 2 for an estimation and the average power requirements). Only further research will be able to determine whether dissipation due to real carriers can be sufficiently suppressed for dielectric-based logic to become a reality in the future. Our qualitative considerations seek to motivate further attosecond research in this fascinating direction.

Although the utility of the recently discovered reversible strong-field effects for signal processing will be verified only in the future, their applicability to advancing high-speed solid-state metrology to the petahertz frontier appears to be quite realistic on the basis of the first experiments. Indeed, by making some refinements, the current measured as a function of delay between the injection and drive laser fields in ref. 119 will directly indicate the temporal evolution of the field, the bandwidth of which was ~ 0.2 PHz in the original experiment. Hence, a solid-state petahertz-bandwidth oscilloscope capable of measuring light waveforms (recently demonstrated in the gas phase¹²¹) is within the realm of reality.

Attosecond physics: the next decade

Some 12 years after the first demonstration of a time-resolved measurement with a sub-femtosecond sampling signal¹⁸ (in other words, attosecond metrology), the field of attosecond physics has come of age. Its key tools and techniques have been tried and tested, and are now being rapidly adopted all over the world. It is time to apply our recently gained ability to track and control electrons in atoms, molecules and solids to problems of direct relevance to life, technology and, potentially, medicine. In this Review, we have addressed how controlled light fields and attosecond measurement techniques may be instrumental in pushing the speed frontier of digital electronics. Direct time-domain insight into electronic motion will also be important for understanding the inner workings of the building blocks of life, namely biomolecules and their complexes. Such knowledge will have ramifications for biotechnologies as well as medical therapies, which involve very complicated electron processes in highly complex systems. The next decade will reveal whether attosecond science and technology is capable of rising to this challenge.

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Competing financial interests

The authors declare no competing financial interests.