

# Optical properties of $n$ -doped $\text{Ga}_{1-x}\text{Mn}_x\text{N}$ epitaxial layers grown by metal-organic chemical-vapor deposition in mid and far (5–50 $\mu\text{m}$ ) IR range

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Optical properties of  $n$ -doped (Si) hexagonal  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films ( $x=0.015$ ) grown by metal-organic chemical-vapor deposition (MOCVD) on  $c$ -plane sapphire substrates have been studied by infrared reflectance spectroscopy. The effect of free carriers on GaMnN optical phonons, namely  $E_1(\text{LO})$  and  $E_1(\text{TO})$ , is explored. It is found that the frequency of  $E_1(\text{LO})$  increases with increasing free carrier concentration. The absorption coefficient ( $\alpha$ ) is calculated for the 200–2000  $\text{cm}^{-1}$  range and the maximum value of  $\alpha$  is found to be  $\sim 10^5 \text{ cm}^{-1}$  at a frequency of 560  $\text{cm}^{-1}$ . With increasing free carrier concentration, the FWHM of the absorption peak increased by 35%–40% as compared to an unintentionally doped ( $< 1 \times 10^{16} \text{ cm}^{-3}$ ) film. © 2008 American Vacuum Society.  
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## I. INTRODUCTION

With the development of dilute magnetic semiconductors (DMS) such as GaMnAs, InMnAs, and GaMnN, spintronic devices<sup>1</sup> such as spin  $p$ – $n$  diodes, spin transistors, spin detectors, spin LEDs, etc. are at the center of attention. During the past few years,  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  thin films have attracted great attention in the field of semiconductor spintronics due to the theoretical prediction of high Curie temperatures<sup>2</sup> and experimental reports of room temperature ferromagnetism.<sup>3</sup> Although studies on the magnetic properties of  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  are widely available,<sup>3–7</sup> only a few studies on the optical properties of  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  epitaxial films, especially in the far infrared (FIR) and mid infrared (MIR) regions, have been reported.<sup>5,8,9</sup> Designing such spintronic and opto-electronic devices based on  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  requires a broader understanding of optical and electrical properties of epitaxial films, which are still rare in the literature. In a recent paper, the optical properties of undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  epitaxial films grown by metal-organic chemical-vapor depositions (MOCVD) were presented.<sup>8</sup> In this study, the optical properties of  $n$ -doped (Si)  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  are investigated using IR reflection spectroscopy. The focus of this article includes a study of the behavior of high frequency dielectric constant  $\epsilon_\infty$  and optical phonon modes [ $E_1(\text{TO})$  and  $E_1(\text{LO})$ ] in  $n$ -doped (Si)  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  epitaxial films deposited on sap-

phire substrates and a comparison of optical properties of doped and undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  epitaxial films and GaN films in the IR range of 200–2000  $\text{cm}^{-1}$  (5–50  $\mu\text{m}$ ). In addition, the IR absorption coefficient in the range of 200–2000  $\text{cm}^{-1}$  (5–50  $\mu\text{m}$ ), which is very important for IR device development, is also discussed.

## II. EXPERIMENT

Three  $n$ -doped (Si) hexagonal  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  epitaxial films, denoted as 1216m ( $0.2 \times 10^{18} \text{ cm}^{-3}$ ), 1218m ( $1.8 \times 10^{18} \text{ cm}^{-3}$ ), and 1221m ( $2.1 \times 10^{18} \text{ cm}^{-3}$ ), and one undoped hexagonal  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  film, 1215m ( $< 1 \times 10^{16} \text{ cm}^{-3}$ ), were used in this study. The manganese composition,  $x$ , was kept at  $x=0.015$  (1.5%) for all four samples. The  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films, 1216 and 1218m, were deposited on  $n$ -GaN/GaN/AlN/sapphire templates while the  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films, 1221 and 1215m, were deposited on GaN/AlN/sapphire templates. The thicknesses of the GaN epilayer, the  $n$ -GaN epilayer, and the AlN buffer layer were  $\sim 1.8 \mu\text{m}$ ,  $\sim 300 \text{ nm}$ , and  $\sim 20 \text{ nm}$ .  $C$ -plane sapphire was used as the substrate material. The epilayers were deposited using a customized GaN MOCVD reactor with a vertical injection system. Ammonia, tri-methyl gallium, bis-cyclopentadienyl manganese ( $\text{Cp}_2\text{Mn}$ ), and silane ( $\text{SiH}_4$ ) were used as the nitrogen, gallium, manganese, and  $n$ -dopant sources, respectively, for the growth of  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films. The concentration of the incorporated Mn was controlled by the molar flow of Mn entering the reactor. Additional details of the growth pro-

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cess were reported elsewhere.<sup>4</sup> Near normal incidence ( $\sim 8^\circ$ ) IR reflection measurements at room temperature were performed over the frequency range of 200–2000  $\text{cm}^{-1}$  (5–50  $\mu\text{m}$ ) using a Perkin-Elmer system 2000 fast Fourier transform infrared spectrometer (FTIR). The IR reflection spectra were taken under  $s$ -polarized and near normal ( $\sim 8^\circ$ ) incident light arrangement to minimize the effect of anisotropy of the hexagonal  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  film.

The dielectric function of doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films in the IR region is predominantly determined by the phonon and the free carrier contributions. The phonon contribution arises from local lattice vibrations under the propagating electric field of the incident light. This can be modeled using a Lorentz oscillator. The free carrier plasma contribution is due to the interaction of free carriers with the electric field of the incidence light. It can be modeled using a classical Drude model approximation. Hence, a complete but simple model for the dielectric function of doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films can be presented as in Eq. (1) for IR region,<sup>10,11</sup>

$$\varepsilon(\omega, n) = \varepsilon_\infty \left[ 1 + \frac{\omega_{\text{LO}}^2 - \omega_{\text{TO}}^2}{\omega_{\text{TO}}^2 - \omega^2 - i\omega\Gamma} - \frac{\omega_p^2(n)}{\omega^2 + i\omega\gamma_p} \right], \quad (1)$$

where  $\varepsilon_\infty$  is the high-frequency dielectric constant, and  $\omega_{\text{LO}}$ ,  $\omega_{\text{TO}}$ , and  $\Gamma$  are the longitudinal (LO) frequency, transverse (TO) frequency, and the broadening constant of the  $E_1$  phonon while  $\omega_p$  and  $\gamma_p$  are the plasma frequency and its damping constant. Moreover, this model addresses the phonon-plasmon coupling. Our recent study<sup>8</sup> on the optical properties of undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  in the IR region shows that considering only  $E_1$  phonon modes in the dielectric model can accurately predict the experimental IR reflection spectra. Therefore, only the  $E_1$  phonon modes (LO and TO) were considered for the lattice vibration contribution.

The transfer matrix method was used to calculate IR reflectance spectra from the multilayer structures.<sup>12</sup> Electric fields in each thin film layer can be calculated using the interface matrix [Eq. (2)] between the  $(j-1)$ th and the  $j$ th layers and the propagation matrix [Eq. (3)] in the  $j$ th layer:

$$T_{j-1,j} = \frac{1}{2\sqrt{\varepsilon_j}} \begin{bmatrix} (\sqrt{\varepsilon_j} + \sqrt{\varepsilon_{j-1}}) & (\sqrt{\varepsilon_j} - \sqrt{\varepsilon_{j-1}}) \\ (\sqrt{\varepsilon_j} - \sqrt{\varepsilon_{j-1}}) & (\sqrt{\varepsilon_j} + \sqrt{\varepsilon_{j-1}}) \end{bmatrix}, \quad (2)$$

$$D_j = \begin{bmatrix} \exp(i2\pi\sqrt{\varepsilon_j}d_j/\lambda) & 0 \\ 0 & \exp(-i2\pi\sqrt{\varepsilon_j}d_j/\lambda) \end{bmatrix}, \quad (3)$$

where  $\varepsilon_j$  is the dielectric function of the  $j$ th layer,  $d_j$  is the thickness of the  $j$ th layer, and  $\lambda$  is the wavelength of the incident light. Light propagation in the whole structure can be expressed by a single matrix obtained by multiplying the interface and the propagation matrices of the multilayer structure, which allows the reflectance coefficient for the whole structure to be easily calculated. A five phase model (air/ $\text{Ga}_{1-x}\text{Mn}_x\text{N}$ /n-GaN/GaN/sapphire) was used to model IR reflections on 1216 and 1218m while the IR reflection spectra for 1221 and 1215m were modeled using a four phase model (air/ $\text{Ga}_{1-x}\text{Mn}_x\text{N}$ /GaN/sapphire). Note the additional  $n$ -doped GaN layer in 1216 and 1218m. The effect

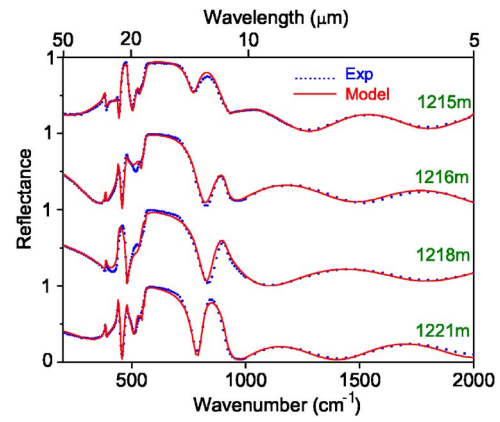


FIG. 1. Experimental infrared reflectance spectra (dotted lines) of the  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films on sapphire substrates and the best fit using Eq. (1) (solid lines). For clarity, each spectrum is successively shifted by 1.0 in the vertical direction.

of the AlN buffer layer on IR reflection was found to be negligible and was ignored in the fitting process since the layer thickness is very small when compared to the other layers. A nonlinear fitting algorithm, Levenberg-Marquardt,<sup>13</sup> was used to extract the best fit parameters for modeling the experimental IR reflection of the  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$ . Initially, IR reflection spectra of the sapphire substrate and the sapphire/GaN template were fitted to the modeled reflection spectra to extract the parameters for the sapphire substrate and the GaN layer. Later, those parameters were fixed during the  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  IR reflection fitting.

### III. RESULTS AND DISCUSSION

Optical constants  $\varepsilon_\infty$ ,  $\omega_{\text{LO}}$ ,  $\omega_{\text{TO}}$ ,  $\Gamma$ ,  $\omega_p$ , and  $\gamma_p$  for  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films were extracted by fitting the experimental IR reflectance spectra. The experimental and modeled IR reflection spectra from 200 to 2000  $\text{cm}^{-1}$  (5–5  $\mu\text{m}$ ) are shown in Fig. 1. Parameters for doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films are listed in Table I along with an undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  film parameters for comparison. The  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  film thicknesses in samples 1215, 1216, 1218, and 1221m were found to be 1765, 1252, 424, and 1335 nm, respectively. The high frequency dielectric constant,  $\varepsilon_\infty$ , for  $n$ -doped and undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films did not vary significantly and remained around 5.2. The free carrier concentration,  $n$ , was calculated using Eq. (4):

$$\omega_p = \left[ \frac{ne^2}{m^* \varepsilon_\infty \varepsilon_0} \right]^{1/2}, \quad (4)$$

where  $\omega_p$  is the plasma frequency and was obtained from the fitting,  $e$  is electron charge,  $m^*$  is the electron effective mass, and  $\varepsilon_0$  is permittivity of free space.  $m^*$  was taken as  $0.2m_0$  where  $m_0$  is the free electron mass. Plasma frequencies for the three  $n$ -doped films, 1216, 1218, and 1221m, are 130, 380, and 422  $\text{cm}^{-1}$ , respectively. From these plasma frequencies, the calculated free carrier concentrations for 1216, 1218, and 1221m are  $\sim 0.2$ ,  $\sim 1.8$ , and  $\sim 2.1 \times 10^{18} \text{ cm}^{-3}$ , respectively. As previously shown, the frequency of  $E_1(\text{TO})$

TABLE I. Parameters obtained from the best fits of IR spectra and sample information. Sample numbers, high frequency dielectric constant ( $\epsilon_\infty$ ),  $E_1(\text{LO})$  and  $E_1(\text{TO})$  mode frequencies, damping constant of  $E_1$  phonon ( $\Gamma$ ), and frequency and damping constant of the plasma oscillator ( $\omega_p$ ,  $\gamma_p$ ). Free carrier concentration,  $n$ , was derived from the plasma frequency. Mn composition,  $x$ , is 1.5% for all four films. Fitting errors are given in parentheses.

Samples	$\epsilon_\infty$	$\omega_{\text{LO}}$ ( $\text{cm}^{-1}$ )	$\omega_{\text{TO}}$ ( $\text{cm}^{-1}$ )	$\Gamma$ ( $\text{cm}^{-1}$ )	$\omega_p$ ( $\text{cm}^{-1}$ )	$\gamma_p$ ( $\text{cm}^{-1}$ )	$n$ ( $10^{18} \text{ cm}^{-3}$ )
1215m	5.22(0.04)	745(1)	564(1)	9.6(0.3)	N/A	N/A	<0.01
1216m	5.17(0.04)	745(2)	561(1)	6.5(1.1)	130(20)	150(90)	0.2
1218m	5.20(0.10)	747(5)	563(1)	8.0(1.9)	366(24)	130(57)	1.8
1221m	5.16(0.05)	754(2)	562(1)	8.09(1.3)	407(10)	387(32)	2.1

in undoped Ga<sub>1-x</sub>Mn<sub>x</sub>N shifts linearly with Mn composition<sup>8</sup> and was found to be at  $564 \text{ cm}^{-1}$  for 1.5% Mn concentration. However, the frequency of  $E_1(\text{TO})$  in Si doped Ga<sub>1-x</sub>Mn<sub>x</sub>N films ( $0.02-2.1 \times 10^{18} \text{ cm}^{-3}$ ,  $x=0.015$ ) was found to be slightly smaller than that of undoped Ga<sub>1-x</sub>Mn<sub>x</sub>N (see Table I). A slight decrease in  $E_1(\text{TO})$  frequency in GaN with increasing doping concentration can be seen in the work reported by Kasic *et al.*;<sup>10</sup> however, Li *et al.*<sup>14</sup> have seen a slight increase in  $E_1(\text{TO})$  frequency with increasing doping concentration in GaN. This can be due to the extra strain in the lattice introduced by Si dopants and different film thicknesses. The  $E_1(\text{LO})$  frequencies for both undoped (1215m,  $<1 \times 10^{16} \text{ cm}^{-3}$ ) and low doped (1216m,  $0.2 \times 10^{18} \text{ cm}^{-3}$ ) Ga<sub>1-x</sub>Mn<sub>x</sub>N films are at  $\sim 745 \text{ cm}^{-1}$ , which is slightly higher than the reported values for GaN: 742.1, 738.4, and  $737.5 \text{ cm}^{-1}$  by Kasic and Schubert,<sup>10</sup> and  $741 \text{ cm}^{-1}$  by Harima.<sup>15</sup> The  $E_1(\text{LO})$  frequencies for samples 1218 and 1221m shifted to higher frequencies due to the stronger LO-phonon and plasmon coupling (LPP). When the plasma frequency gets closer to the LO-phonon frequency, the coupling gets stronger and therefore LO frequency shifts to higher frequency.<sup>11</sup>

The coupling of longitudinal optical phonons [ $E_1(\text{LO})$  and  $A_1(\text{LO})$ ] and plasmons, LPP modes, is expected when free carriers are present in the material and is stronger when the plasma frequency,  $\omega_p$ , is near the longitudinal optical phonon (LO) frequencies. The behaviors of the couple modes between  $E_1(\text{LO})$  and the plasmon ( $E_1\text{-LPP}$ ) for *n*-doped films 1216, 1218, and 1221m are shown in Figs. 2(a)–2(c), respectively. Frequencies of  $E_1\text{-LPP}^+$  are 750, 800, and  $810 \text{ cm}^{-1}$  while frequencies of  $E_1\text{-LPP}^-$  are 85, 260, and  $255 \text{ cm}^{-1}$  for samples 1216, 1218, and 1221m, respectively. The LPP mode frequency can be theoretically calculated by setting the dielectric function [Eq. (1)] to zero in the limit of zero damping and is given as follows:

$$\omega_{\pm} = \frac{\omega_{\text{LO}}^2 + \omega_p^2}{2} \pm \left[ \frac{(\omega_{\text{LO}}^2 + \omega_p^2)^2}{4} - \omega_p^2 \omega_{\text{TO}}^2 \right]^{1/2}. \quad (5)$$

Figure 2(d) shows the theoretically predicted  $E_1\text{-LPP}$  mode behavior and experimentally deduced  $E_1\text{-LPP}$  frequencies as free carrier concentration increases. Generally, the  $\text{LPP}^+$  mode reaches  $\omega_{\text{LO}}$  and the  $\text{LPP}^-$  mode reaches zero as the free carrier concentration reaches zero [see the two solid

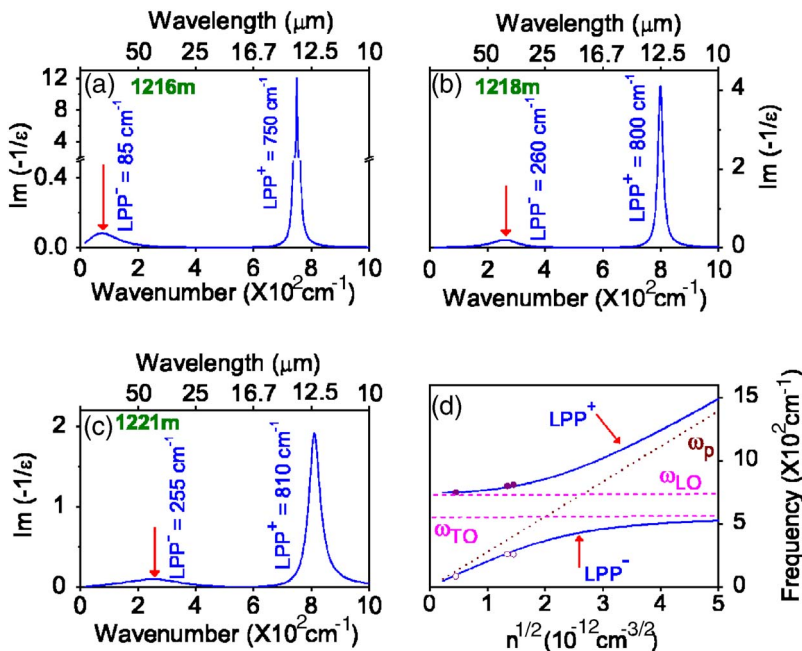


FIG. 2.  $\text{Im}(-1/\epsilon)$  as function of frequency is shown for three doped Ga<sub>1-x</sub>Mn<sub>x</sub>N samples: (a) 1216m, (b) 1218m, and (c) 1221m. Plasmon and phonon coupling modes,  $E_1\text{-LPP}^+$  and  $E_1\text{-LPP}^-$  are clearly visible. A comparison of experimentally derived and theoretically predicted  $E_1\text{-LPP}$  mode behavior with square root of free carrier concentration is shown in (d). Solid lines: theoretically predicted behavior of  $E_1\text{-LPP}^+$  and  $E_1\text{-LPP}^-$ , Solid dots and white circles: experimentally obtained  $E_1\text{-LPP}$  mode values, Dashed lines:  $\omega_{\text{TO}}$  and  $\omega_{\text{LO}}$ . Dotted line:  $\omega_p$  variation.

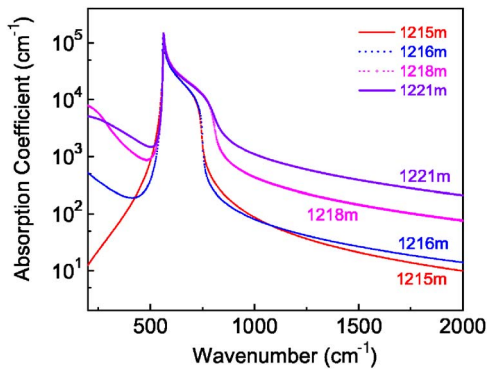


FIG. 3. The derived absorption coefficients,  $\alpha$  for all four  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films in  $200\text{--}2000\text{ cm}^{-1}$  ( $50\text{--}10\text{ }\mu\text{m}$ ). The absorption coefficient reaches its maximum at  $550\text{ cm}^{-1}$ . The width of the absorption peak has increased by  $35\%\text{--}40\%$  in higher doped films ( $>1 \times 10^{18}\text{ cm}^{-3}$ ).

lines in Fig. 2(d)]. Therefore, the  $\text{LPP}^+$  mode shows  $\omega_{\text{TO}}$  phononlike behavior at low doping. As the free carrier concentration increases, the  $\text{LPP}^+$  mode approaches  $\omega_p$  while the  $\text{LPP}^-$  mode approaches  $\omega_{\text{TO}}$  (see the two solid lines). Therefore, the  $\text{LPP}^+$  mode shows plasmonlike behavior for higher doping concentrations.

A knowledge of IR absorption coefficient of materials,  $\alpha$ , is important for designing infrared detectors and  $\alpha$  can be calculated using Eq. (6):

$$\alpha = \frac{4\pi \text{Im}(\sqrt{\epsilon})}{\lambda}, \quad (6)$$

where  $\text{Im}(\sqrt{\epsilon})$  is the imaginary part of the square root of the dielectric function and  $\lambda$  is the wavelength. The calculated absorption coefficients for all four films are shown in Fig. 3 in the  $200\text{--}2000\text{ cm}^{-1}$  range ( $5\text{--}50\text{ }\mu\text{m}$ ). The absorption coefficient peaks in the GaN Reststrahlen band and reaches its maximum,  $1 \times 10^5\text{ cm}^{-1}$ , around the frequency  $560\text{ cm}^{-1}$ . The absorption peak gets broader with increasing free carrier concentration. For highly doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films, the line width of the absorption peak has increased by about  $35\%\text{--}40\%$  with respect to undoped or low doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  films. This broadening is due to the  $\text{LPP}^+$  mode shifting to higher frequency with increasing doping. At frequency  $200\text{ cm}^{-1}$  ( $50\text{ }\mu\text{m}$ ), absorption has increased from  $12\text{ cm}^{-1}$  to roughly  $7500\text{ cm}^{-1}$  as the free carrier concentration was increased to  $2.1 \times 10^{18}\text{ cm}^{-3}$  from undoped ( $<1 \times 10^{16}\text{ cm}^{-3}$ ). The increase in  $\alpha$  at wave number  $200\text{ cm}^{-1}$  is an advantage for far infrared detectors. In addition, in the

short wavelength region ( $1000\text{--}2000\text{ cm}^{-1}$ ),  $\alpha$  has increased by a factor of 5, at least, the highest doped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  film. In general,  $\alpha$  increases with increasing free carrier concentration.

#### IV. CONCLUSIONS

The high frequency dielectric constant,  $\epsilon_\infty$ , and optical phonon modes,  $E_1(\text{LO})$  and  $E_1(\text{TO})$ , were investigated. High frequency dielectric constant,  $\epsilon_\infty$ , in  $n$ -doped  $\text{Ga}_{0.985}\text{Mn}_{0.015}\text{N}$  films is between 5.2 and 5.3, which is close to the reported values of undoped  $\text{Ga}_{1-x}\text{Mn}_x\text{N}$  (Ref. 8) and GaN.<sup>15,16</sup> The frequencies of  $E_1(\text{TO})$  of doped and undoped  $\text{Ga}_{0.985}\text{Mn}_{0.015}\text{N}$  films do not show a significant difference, whereas  $E_1(\text{LO})$  frequency increases with increasing free carrier concentrations for the investigated range of  $2 \times 10^{17}$  to  $3 \times 10^{18}\text{ cm}^{-3}$ .

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