



Fall 2017

Physics 8100 - Electromagnetic Theory I



N. Dietz

Assignment # 8 (due to Monday, November 27, 2017)

Problem 1: (20 points)

A line charge density $\sigma(\vartheta) = K \cdot \cos(\vartheta)$ is glued over the surface of a spherical shell of radius R , where K is a constant. Find the resulting potential inside and outside the sphere.

Problem 2: (20 points)

A line charge density is distributed on the z -axis from $z = -a$ to $z = a$. Using the method of Green's function, find the potential for $r > a$ to the order of $(a/r)^5$.

Problem 3: (20 points)

A sphere of radius R carries the charge density

$$\rho(\vec{r}) = \frac{A(1 - \cos\theta)}{r^2},$$

where A is a constant. Find the potential far from the sphere.

Problem 4: (20 points)

Find the electric field inside and outside a dielectric sphere of radius R that has a uniform polarization vector \mathbf{P} .

Problem 5: (20 points)

A plane interface separates two semi-infinite dielectric media with dielectric constants ϵ_1 and ϵ_2 . The surface may be taken as the plane $z = 0$. A charge q in the dielectric ϵ_1 is at $(0, 0, a)$ and a charge $-q$ in the dielectric ϵ_2 is at $(0, 0, -a)$. Find the forces between these two charges (hint: use the method of images and apply the proper boundary conditions).