



Fall 2017

# Physics 8100 - Electromagnetic Theory I



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## Assignment # 3 (due to Monday, October 02, 2017)

- 1) **Problem 1.4**, Jackson textbook (page 51): Each of three charged spheres of radius  $a$ , one conducting, one having an uniform charge density within its volume, and one having a spherically symmetric charge density that varies radially as  $r^n$  ( $n > -3$ ), has the total charge  $Q$ . Use the Gauss's theorem to obtain the electric fields both inside and outside each sphere. Sketch the behavior of the fields as a function of radius for the first two spheres, and for the third with  $n=-2, +2$ .
- 2) Find the potential and the electric field strength along the axis of a thin uniformly charged circular disc of radius  $R$  and total charge  $q$ . Show that the normal component of the field changes by  $\sigma/\epsilon_0$  on passing through the surface of the disc. Consider the field at large distances from the disc.
- 3) Consider a spherically symmetric charge distribution  $\rho=\rho(r)$ . By dividing the charge distribution into spherical shells, find the potential and the electric field strength in terms of  $\rho(r)$  (write down the potential and the field in the form of an integral with respect to  $r$ ).
- 4) A line conductor of length  $L$  and total charge  $Q$  lies on the  $x$ -axis with one end on the origin. Find the electric potential and the electric field at any point on the  $x$ -axis for  $x > L$ .
- 5) Two infinite parallel plates separated by a distance  $s$  are at the potentials 'zero' and  $V_0$ .
  - a) Use Poisson's equation to find the potential in the region between the plates where the space charge density  $\rho$  is a linear function of  $x$  – for instance  $\rho(x) = \rho_0 \cdot \frac{x}{s}$   
The distance is measured from the plate at 'zero' potential.
  - b) Find the surface charge densities on the plates.